# Does Strategic Ability Affect Efficiency? Evidence from Electricity Markets

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	Firm 1	Firm 2
Identity	Split from former	Municipal Utility
	vertically integrated utility	
Physical	13 generating units	2 generating units
assets	pprox 18,000 MW of natural gas,	pprox 500 MW of natural gas
	coal and nuclear	
Trader's	1y "Director of Energy Trading"	2ys trading desk at another firm
previous	4ys "Energy Trader"	10ys "Superv. of System Operations"
experience	3ys natural gas transportation	8ys "System Operator"
	& exchange firm	4ys "System Operations Dispatcher"
		4ys "Generation Control Operator"

## Motivation

Efficiency concerns from an antitrust perspective: large firms

- Exercise market power
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Should we worry about how **small** firms compete?

Can firms compete in a way that creates inefficiency, in addition to those related to market power? (i.e. prevents least-cost dispatch)

Can differences in sophistication of pricing strategies cause inefficiencies?

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Can differences in sophistication of pricing strategies cause inefficiencies?

#### This paper:

What if all real-world firms were to engage in <u>some</u> strategic thinking, but some "fall short" of playing Nash equilibrium?

Heterogeneity in level of strategic thinking?

# Strategic Sophistication and Efficiency

- (Standard) "Sophisticated" Nash equilibrium bidding leads to inefficiency, aka "market power".
- (Less Studied) Low level strategic thinking also inefficient
  - Hortaçsu and Puller (2008) study electricity auctions

Rich theory/lab literature on bounded rationality theory: Level-*k*, Cognitive Hierarchy, QRE.

- In I.O., we have seen work on demand but almost nothing on supply.
- More in general, almost no application of level-*k*, CH, and QRE using field data.

Why? Identification.

# Strategic Sophistication and Efficiency

#### Consider the "normal" I.O. approach

- $\bullet \ \ Differentiated \ product \ industries: MC \rightarrow prices \\$
- Auctions: valuations → bids

#### Solution: field data on marginal cost

Enter electricity markets...

## This paper

- Same context as HP: bidding in the Texas electricity market
- Our strategy
  - Embed a Cognitive Hierarchy (CH) model into a structural model of bidding
  - Exploit a dataset with bids and marginal costs to estimate levels of strategic sophistication
- Why? (aka, what is new relative to HP?)
  - How heterogeneous is sophistication?
  - What is the impact of strategic sophistication on efficiency?
  - What are the (private) returns to strategic sophistication?
- Bonus: Ability to calculate counterfactuals
  - In multi-unit auctions, solving for Nash equilibria is difficult/impossible (fixed point in function space)
  - The structure of the CH model makes finding equilibrium "easy" (sequence of best-responses)

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- Sould mergers that increase strategic sophistication, but do not create cost synergies, increase efficiency?
  - Yes, but only if small firms involved; otherwise concentration effect dominates.

#### Literature

- Theory and lab: Costa-Gomez, Crawford and Broseta (2001), Crawford and Iriberri (2007), Camerer et al (2004), McKelvey and Palfrey (1995), Nagel (1995), Stahl and Wilson (1995), Gill and Prowse (2016).
- Empirical/field: Hortaçsu and Puller (2008), Gillen (2010), Goldfarb and Xiao (2011), An (2013).
- Electricity markets: Doraszelski, Lewis, and Pakes (2016), Fabra and Reguant (2014), Bushnell, Mansur and Saravia (2008), Sweeting (2007), Wolak (2003), Borenstein, Bushnell and Wolak (2002), Wolfram (1998).
- **Productivity differences across firms**: Syverson (2004), Hsieh and Klenow (2009), Bloom and Van Reenen (2007).
- Behavioral supply: Romer (2006), Massey and Thaler (2013), Ellison, Snyder, and Zhang (2016), DellaVigna and Gentzkow (2017).

#### Outline

- Institutional setting
- A Model of Non-Equilibrium Bidding Behavior
- Oata and Estimation
- 4 Counterfactuals: Increasing Sophistication

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**Institutional Setting** 

## Texas Electricity Market - Early Years

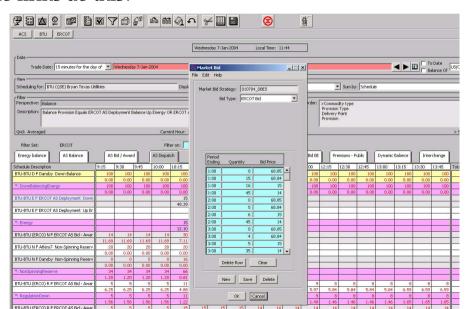
#### Timeline of Market Operations:

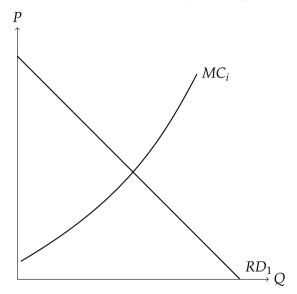
- Generating firms sign bilateral trades with firms that serve customers
- Day-ahead: One day before production and consumption, generating firms schedule a fixed quantity of production for each hour of the following day ('day-ahead schedule')
- Day-of: shocks can occur (e.g. hotter July afternoon than anticipated)
- 'Balancing Market' to ensure supply and demand balance at every point in time

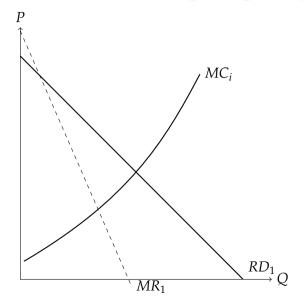
## **Balancing Market Auction**

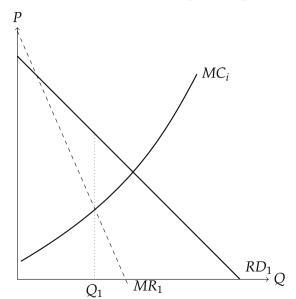
- Generation firms submit hourly bids to change production relative to their 'day-ahead schedule'
  - Bids are monotonic step functions (up to 40 elbow points) for portfolio of firm's generators
- Demand is perfectly inelastic
- Uniform-price auction that clears every 15-minute interval with hourly bids
- Accounts for 2-5% of all power traded

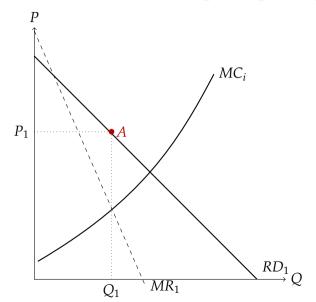
#### How do firms do this?

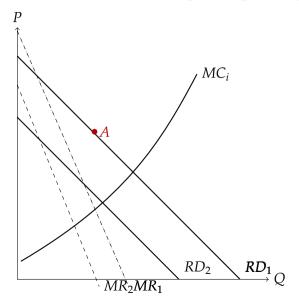


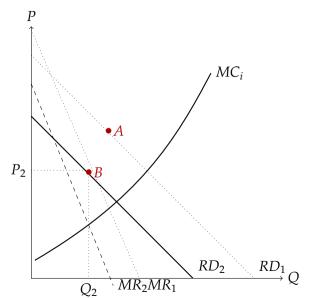


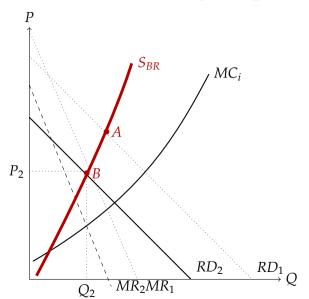




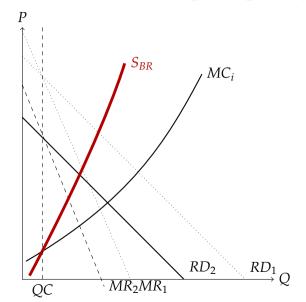




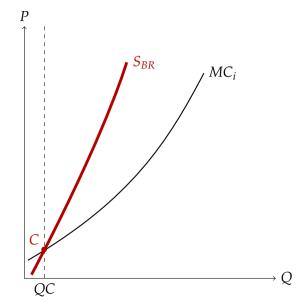


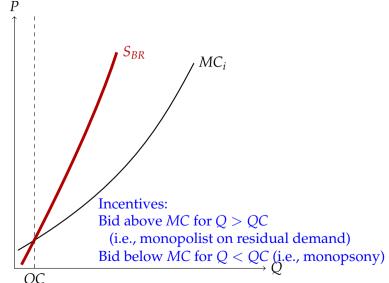


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## Data



#### Data



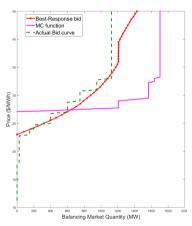
For each hourly auction, we have data on:

- Demand perfectly inelastic balancing demand
- Bids each firm's hourly firm-level ("portfolio") bids
- Marginal costs each firm's hourly MC of supplying balancing power for plants that are "turned on" MC Details MC Figure

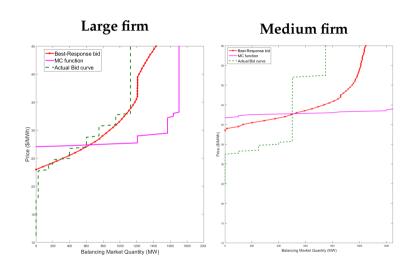
We focus on the 6–6:15pm periods with no transmission congestion.

### What do we observe?

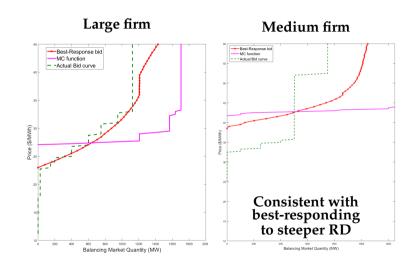




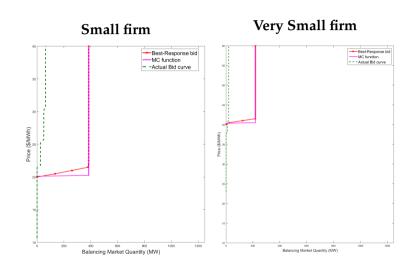
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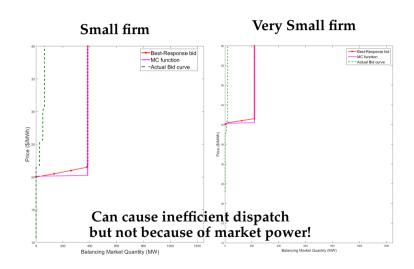
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#### What do we observe?



#### What do we observe?



# Summarizing Performance Across Firms

	Percent of Potential
Firm	Profits Achieved
Reliant	79%
City of Bryan	45%
Tenaska Gateway Partners	41%
TXU	39%
Calpine Corp	37%
Cogen Lyondell Inc	16%
Lamar Power Partners	15%
City of Garland	13%
West Texas Utilities	8%
Central Power and Light	8%
Guadalupe Power Partners	6%
Tenaska Frontier Partners	5%

## Ruling Out Alternative Explanations

- Do bidding rules prevent firms from submitting ex post "best response" bids?
  - No! → "Simple bidding rule"
- Are the <u>dollar stakes</u> large enough to justify the fixed costs of submitting the "right" bids?
  - Money-on-the-table: between 3 and 18 million dollars per year.
- Startup costs?
  - All the units we consider in MC are already "on".
- Adjustment costs?
  - Flexible natural gas units often are marginal.
  - Inconsistent with Medium firm's bid for quantities below contract position.
  - "Bid-ask" spread smaller for firms closer to best-response bidding despite having similar technology.

## Ruling Out Alternative Explanations

- Is capacity overstated?: No, and even if it did it wouldn't be a problem when *decreasing* generation.
- <u>Transmission constraints</u>: HP find cannot explain deviations.
- <u>Collusion</u>: would be small players; monetary transfers unlikely.

# A Model to Explain this Bidding Behavior:

"Cognitive Hierarchy"

- Pick a number between 0 and 100
- Winner is player with number closest to  $\frac{2}{3}$  of average
- What is your number?

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- Level-1 thinking: If all other players pick 100, I should pick 67.

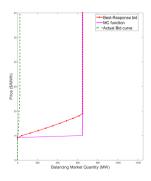
- Pick a number between 0 and 100
- Winner is player with number closest to  $\frac{2}{3}$  of average
- What is your number?
- Level-1 thinking: If all other players pick 100, I should pick 67.
- Level-2 thinking: If all other players use above reasoning, I should pick 45.

- Pick a number between 0 and 100
- Winner is player with number closest to  $\frac{2}{3}$  of average
- What is your number?
- Level-1 thinking: If all other players pick 100, I should pick 67.
- Level-2 thinking: If all other players use above reasoning, I should pick 45.
- Level-3 thinking: If all other players use above reasoning....
- ...

- Pick a number between 0 and 100
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- What is your number?
- Level-1 thinking: If all other players pick 100, I should pick 67.
- Level-2 thinking: If all other players use above reasoning, I should pick 45.
- Level-3 thinking: If all other players use above reasoning....
  - ..
- Only rational and consistent choice is to choose 0
- People playing a game can have different levels of strategic thinking

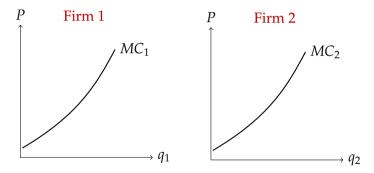
## Cognitive Hierarchy Applied to this Market

- Relaxes Nash assumption of 'mutually consistent beliefs'.
- Players differ in level of strategic thinking.
  - $k_i \in \{0, ..., K\}$
- Level-0 players are non-strategic (Important assumption, I'll discuss it in detail in a couple of minutes)



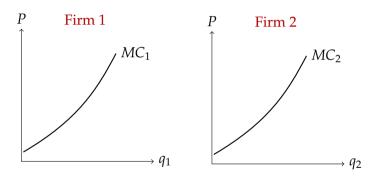
# Cognitive Hierarchy Applied to this Market

- Players level-1 to level-*k* are increasingly more strategic
  - level 1: assume *all* rivals are level 0. Best-respond to these beliefs.
  - level 2: assume rivals are distributed between level 0 and level 1. Best respond to these beliefs.
  - ...
  - level k: assume rivals are distributed between level 0 and level k-1. Best respond to these beliefs.
- Firms beliefs about their rivals' level of strategic thinking is a function of characteristics of those rivals (e.g. size)

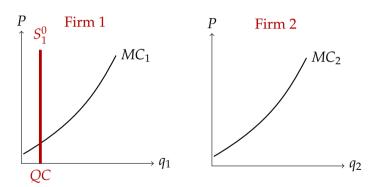




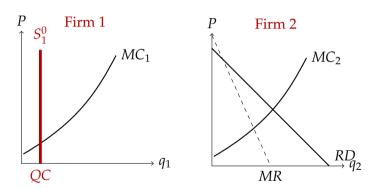
Assume  $F_2$  believes  $F_1$  to be type-0



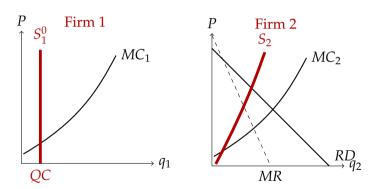
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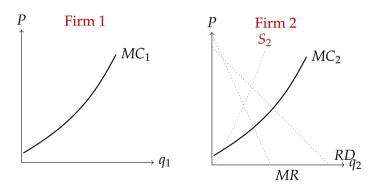
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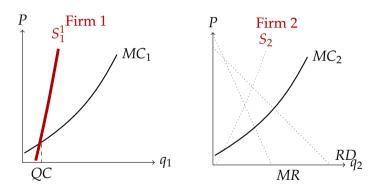
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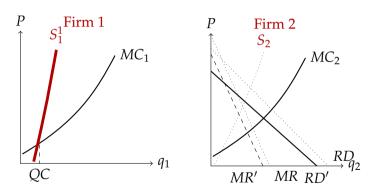
Assume  $F_2$  believes  $F_1$  to be type-1



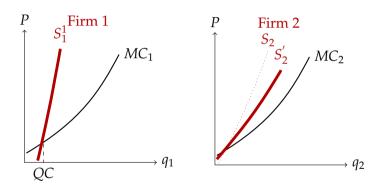
Assume  $F_2$  believes  $F_1$  to be type-1



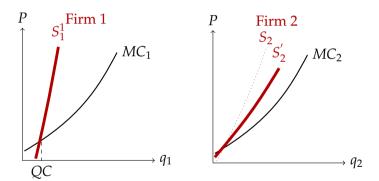
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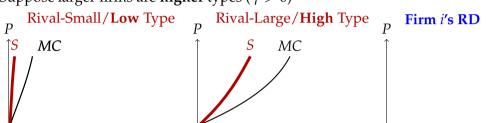


Higher-type rivals rotate RD and induce more competitive bidding

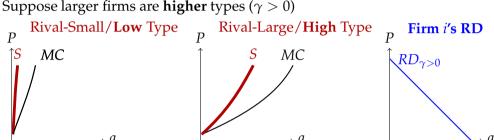




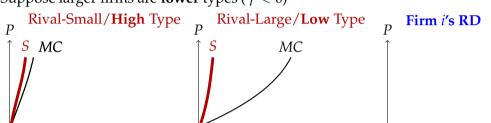
Suppose larger firms are **higher** types ( $\gamma > 0$ )



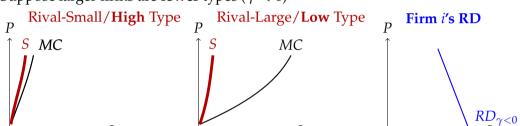
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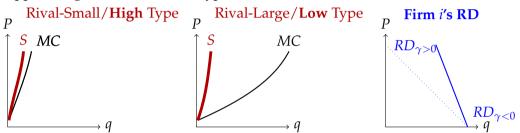
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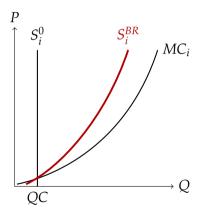
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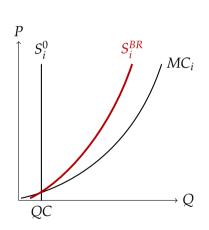
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Is i's bid more consistent with  $RD_{\gamma>0}$  or  $RD_{\gamma<0}$ ?

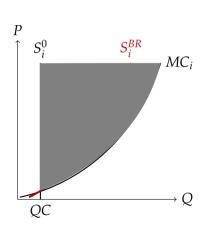


In general, level-0s are non-strategic players. In our setting, this can be

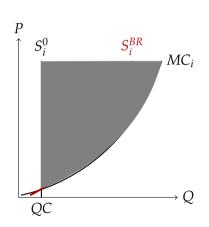


Bid randomly

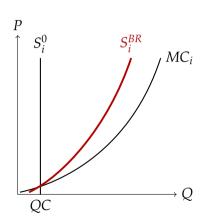
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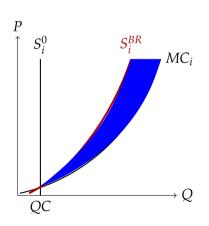
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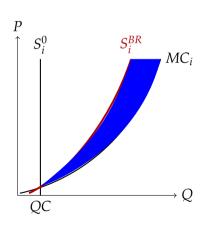
- Bid randomly
  - not observed



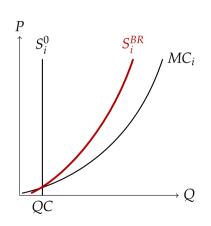
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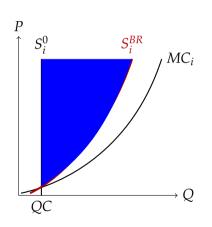
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- Bid vertical

#### More on level-0 firms

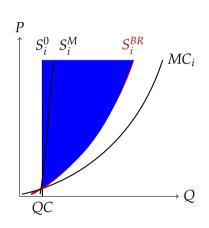
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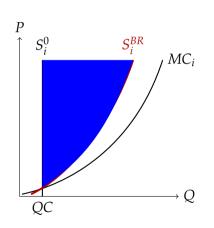
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#### More on level-0 firms

In general, level-0s are non-strategic players. In our setting, this can be



- Bid randomly
  - not observed
- Bid marginal costs
  - bids would have to be flatter than BR, not observed
- Bid vertical
  - higher types would bid flatter and approach BR from the left, as we observe

# Estimation

#### **Estimation: Information**

Firm type:  $k_i \sim Poisson(\hat{\tau}_i)$ ,  $\hat{\tau}_i = \exp(\hat{\gamma}_0 + \hat{\gamma}_1 \operatorname{size}_i)$ .

- $k_i$  is private information
- $\tau_i$  is public information.

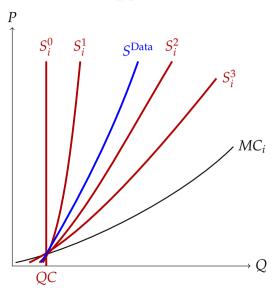
Costs: public information.

 $k_i$  and size $_{-i}$  determine i's beliefs about -i's types.

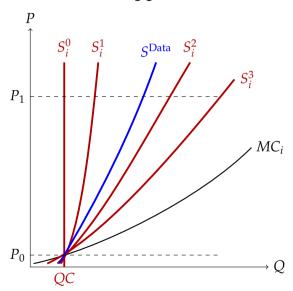
*i* best-responds to those beliefs.

We compute i's best response for each k and minimize the distance between predicted bids and the data.

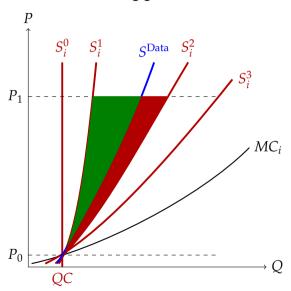
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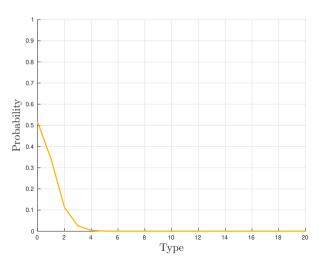


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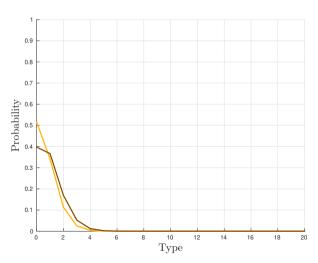


#### **Results**

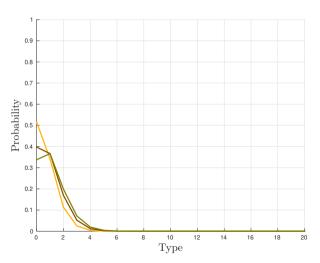
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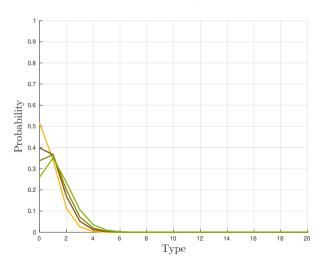
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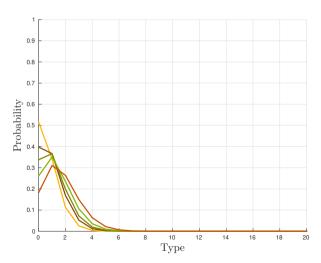
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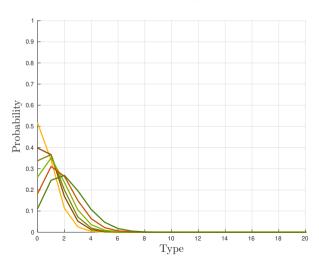
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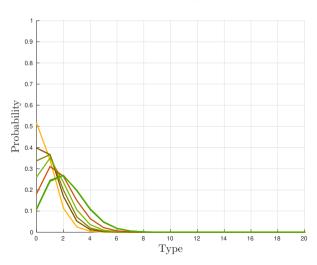
$$k_i \sim Poisson(\hat{\tau}_i), \ \hat{\tau}_i = \exp(\hat{\gamma}_0 + \hat{\gamma}_1 \operatorname{size}_i)$$



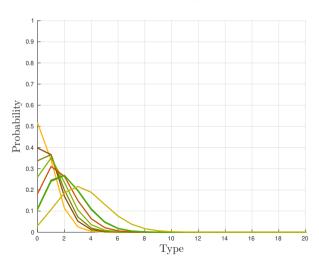
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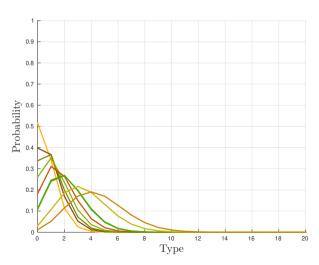
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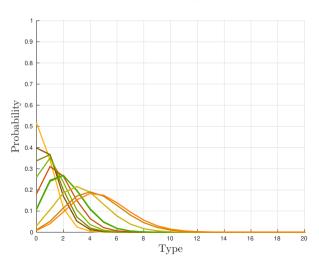
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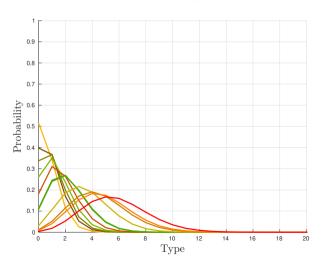
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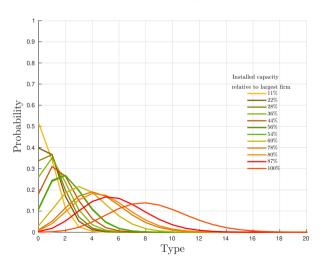
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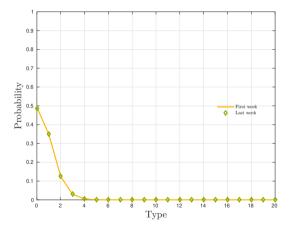
$$k_i \sim Poisson(\hat{\tau}_i), \ \hat{\tau}_i = \exp(\hat{\gamma}_0 + \hat{\gamma}_1 \operatorname{size}_i)$$



## Manager Training Matters

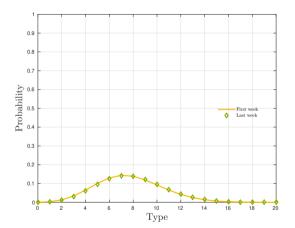
	(1)	(2)	(3)
Constant	-0.726	-0.749	-3.493
	(0.087)	(0.106)	(0.414)
Size	14.594	13.619	3.090
	(1.027)	(1.188)	(0.755)
AAU School		0.376	
		(0.065)	
Econ/Business/Finance degree			5.626
			(1.188)
Number of auctions		99	

#### Learning?



**Small Firm** - Estimated Type Distribution with Learning (*Size* and time trend specification)

#### Learning?



**Big Firm** - Estimated Type Distribution with Learning (*Size* and time trend specification)

▶ More on learning: Quantity offered did not change over time

## Out-of-sample prediction

	Dependent variable: Realized profits				
	(1)	(2)	(3)		
Unilateral BR	0.263***		0.061		
	(0.052)		(0.091)		
СН		0.703***	0.642**		
		(0.136)	(0.211)		
Constant	-64.484	-248.599**	-264.619**		
	(156.308)	(101.941)	(97.348)		
Observations	426	426	426		
$R^2$	0.248	0.561	0.570		

#### Simulations of Changes in Sophistication

- "Consulting Firm"
- Merger

	IN	C side	DE	C side
Counterfactual	Public	Private	Public	Private
Small firms to median				
Above median firms to highest				
Three smallest to median				

	IN	C side	DE	C side
Counterfactual	Public	Private	Public	Private
Small firms to median	-6.95%			
Above median firms to highest				
Three smallest to median				

	IN	C side	DE	C side
Counterfactual	Public	Private	Public	Private
Small firms to median	-6.95%			
Above median firms to highest	-2.71%			
Three smallest to median				

	IN	C side	DE	C side
Counterfactual	Public	Private	Public	Private
Small firms to median	-6.95%			
Above median firms to highest	-2.71%			
Three smallest to median	-4.67%			

	IN	C side	DE	C side
Counterfactual	Public	Private	Public	Private
Small firms to median	-6.95%	-6.22%		
Above median firms to highest	-2.71%	-1.96%		
Three smallest to median	-4.67%	-3.75%		

	IN	C side	DE	C side
Counterfactual	Public	Private	Public	Private
Small firms to median	-6.95%	-6.22%	-18.4%	-17.6%
Above median firms to highest	-2.71%	-1.96%	-13.42%	-12.46%
Three smallest to median	-4.67%	-3.75%	-14.24%	-13.64%

## Mergers that Increase Sophistication

Mergers only reduce generation costs when small firms are involved

	INC side	DEC side
Smallest and largest firms	-2.62%	-6.49%
Median and largest firms	+10.29%	+10.37%
Two largest firms	+18.34%	+48.72%

#### Conclusions and Takeaway Messages

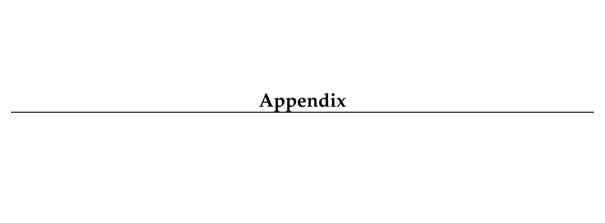
Does heterogeneity in strategic sophistication affect market performance?

- Context: bidding into electricity auctions in Texas.
- First paper using field data to study pricing decisions.
- To model pricing decisions, we embed a CH model into a structural model of bidding.

#### Takeaways:

- Significant heterogeneity in sophistication. Larger firms are more sophisticated than smaller firms.
- ② Does sophistication matter? Yes!
  - Increasing sophistication improves efficiency.
  - Most of the gains come from smaller firms.
- **③** Could mergers that increase sophistication, but do not create cost synergies, increase efficiency?
  - Yes, but only if small firms are involved.





# Main players in generation

Firm	% of installed capacity
TXU	24
Reliant	18
City of San Antonio	8
Central Power & Light	7
City of Austin	6
Calpine	5
Lower Colorado River Authority	4
Lamar Power Partners	4
Guadalupe Power Partners	2
West Texas Utilities	2
Midlothian Energy	2
Dow Chemical	1
Brazos Electric Power Cooperative	1
Others	16

#### Can Firms Do This in Practice?

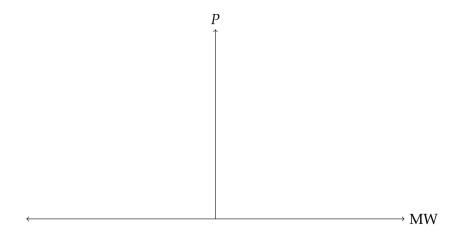
- Grid operator reports aggregate bid function with a 2 day lag
- Simple trading rule
  - Download bid data from 2 days ago
  - Assume rivals do not change their bids
  - Calculate best response to lagged rivals' bids
- Does this outperform actual bidding?
- Answer: Yes and it yields almost the same profits as best response to current rivals' bids

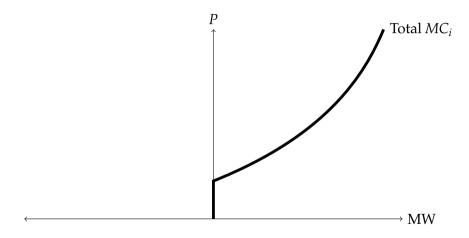
# Firm performance relative to best-responding

	Percent achieved by			
	Actual bids	BR to lagged bids		
Reliant	79%	98.5%		
City of Bryan	45%	100%		
Tenaska Gateway	41%	99.6%		
TXU	39%	96.7%		
Calpine	37%	97.9%		
Cogen Lyondell	16%	100%		
Lamar Power Partners	15%	99.6%		
City of Garland	13%	99.6%		
West Texas Utilities	8%	100%		
Central Power and Light	8%	98.7%		
Guadalupe Power Partners	6%	99%		
Tenaska Frontier	5%	99.3%		

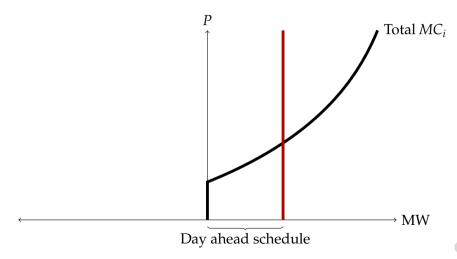
Source: Hortaçsu and Puller (2008). • Back

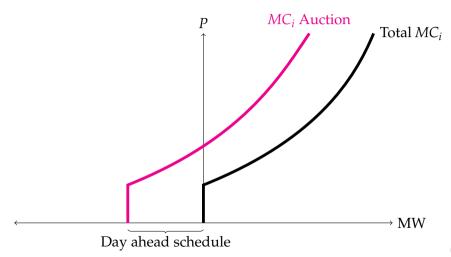
- Each <u>unit's</u> daily capacity & day-ahead schedule
- Marginal Costs for each fossil fuel unit
  - Fuel costs daily natural gas spot prices (NGI) & monthly average coal spot price (EIA)
  - Fuel efficiency average "heat rates" (Henwood)
  - Variable O&M (Henwood)
  - SO2 permit costs (EPA)
- Use coal and gas-fired generating units that are "on" that hour and the daily capacity declaration (Nukes, Wind, Hydro may not have ability to adjust)
- Calculate how much generation from those units is already scheduled == Day-Ahead Schedule











• Market clearing price  $p_t^c$ :

$$\sum_{i=1}^{N} S_{it}(p_t^c, QC_{it}) = D_t(p_t^c) + \varepsilon_t$$
(1)

- Three sources of uncertainty
  - Demand shock  $(\varepsilon_t)$
  - Rival Contract positions ( $QC_{-it}$ )
  - Rival Types  $(k_{-i})$

$$H_{it}(p, \hat{S}_{it}(p); k_i, QC_{it}) \equiv Pr(p_t^c \le p | \hat{S}_{it}(p), k_i, QC_{it})$$
(2)

• Market clearing price  $p_t^c$ :

$$\sum_{i=1}^{N} S_{it}(p_t^c, QC_{it}) = D_t(p_t^c) + \varepsilon_t$$
(1)

- Three sources of uncertainty
  - Demand shock  $(\varepsilon_t)$
  - Rival Contract positions (QC<sub>-it</sub>)
  - Rival Types  $(k_{-i})$

$$H_{it}(p, \hat{S}_{it}(p); k_i, QC_{it}) \equiv Pr(p_t^c \le p | \hat{S}_{it}(p), k_i, QC_{it})$$
 (2)

Combining (1) and (2) and denoting *i*'s private information  $\Omega_{it} \equiv \{k_i, QC_{it}\}$ :

$$H_{it}(p, \hat{S}_{it}(p); \Omega_{it}) = \\ \int_{QC_{-it}, \boldsymbol{l}_{-i}, \varepsilon_t} 1 \left[ \sum_{j \neq i}^{\text{aggregate supply}} \sum_{j \neq i}^{\text{aggregate supply}} \sum_{j \neq i}^{\text{prop}} S_{jt}^l(p, QC_{jt}; k_i) + \hat{S}_{it}(p) \ge D_t(p) + \varepsilon_t \right] dF(QC_{-it}, \boldsymbol{l}_{-i}, \varepsilon_t | \hat{S}_{it}(p), \Omega_{it})$$

 $F(QC_{-it}, l_{-i}, \varepsilon_t | \hat{S}_{it}(p), \Omega_i)$ : the joint density of each source of uncertainty from the perspective of firm i.

Let 
$$\theta_i \equiv \sum_{j \neq i} S^l_{jt}(\cdot; k_i) - \varepsilon \sim \Gamma_i$$
. Back

The firm's problem

$$\max_{\hat{S}_{it}(p)} \int_{\underline{p}}^{\overline{p}} \left( U\left(p \cdot \hat{S}_{it}(p) - C_{it}\left(\hat{S}_{it}(p)\right) - (p - PC_{it})QC_{it}\right) \right) dH_{it}\left(p, \hat{S}_{it}(p); \Omega_{it}\right)$$

Necessary condition for optimality

$$p - C'_{it}(S^*_{it}(p)) = (S^*_{it}(p) - QC_{it}) \frac{H_s(p, S^*_{it}(p); k_i, QC_{it})}{H_p(p, S^*_{it}(p); k_i, QC_{it})}$$
(3)



The firm's problem

$$\max_{\hat{S}_{it}(p)} \int_{\underline{p}}^{\overline{p}} \left( U\left(p \cdot \hat{S}_{it}(p) - C_{it}\left(\hat{S}_{it}(p)\right) - (p - PC_{it})QC_{it}\right) \right) dH_{it}\left(p, \hat{S}_{it}(p); \Omega_{it}\right)$$

Necessary condition for optimality:

$$p - C'_{it}(S^*_{it}(p)) = (S^*_{it}(p) - QC_{it}) \frac{H_s(p, S^*_{it}(p); k_i, QC_{it})}{H_p(p, S^*_{it}(p); k_i, QC_{it})}$$

(3)



- It implies that residual demand is flatter for higher type.
- No more assumptions needed about how private information enters the bid functions.

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$$H_{it}(p, \hat{S}_{it}(p); k = 1, QC_{it}) = \int_{QC_{-it}, l_{-i}, \varepsilon_t} 1(\sum_{j \neq i} S_{jt}^0(p, QC_{jt}) + \hat{S}_{it}^1(p) \ge D_t(p) + \varepsilon_t) dF(QC_{-it}, l_{-i}, \varepsilon_t | \hat{S}_{it}^1(p), k_i = 1, QC_{it})$$

- It implies that residual demand is flatter for higher type.
- No more assumptions needed about how private information enters the bid functions.

$$\begin{split} H_{it}(p, \hat{S}_{it}(p); k = 1, QC_{it}) &= \int_{QC_{-it}, l_{-i}, \varepsilon_{t}} 1(\sum_{j \neq i} S^{0}_{jt}(p, QC_{jt}) + \hat{S}^{1}_{it}(p) \geq \\ &D_{t}(p) + \varepsilon_{t}) dF(QC_{-it}, l_{-i}, \varepsilon_{t} | \hat{S}^{1}_{it}(p), k_{i} = 1, QC_{it}) \\ &= \int_{QC_{-it}, l_{-i}, \varepsilon_{t}} 1(\sum_{j \neq i} \overbrace{QC_{jt}} - \varepsilon_{t} \geq \\ &D_{t}(p) - \hat{S}^{1}_{it}(p)) dF(QC_{-it}, l_{-i}, \varepsilon_{t} | \hat{S}^{1}_{it}(p), k_{i} = 1, QC_{it}) \end{split}$$

- 1 It implies that residual demand is flatter for higher type.
- $\ensuremath{\text{2}}$  No more assumptions needed about how private information enters the bid functions.

$$\begin{split} H_{it}(p, \hat{S}_{it}(p); k = 1, QC_{it}) &= \int_{QC_{-it}, I_{-i}, \varepsilon_{t}} 1(\sum_{j \neq i} S_{jt}^{0}(p, QC_{jt}) + \hat{S}_{it}^{1}(p) \geq \\ &D_{t}(p) + \varepsilon_{t}) dF(QC_{-it}, I_{-i}, \varepsilon_{t} | \hat{S}_{it}^{1}(p), k_{i} = 1, QC_{it}) \\ & \underset{Assumption 1}{\text{Assumption 1}} 1 = \int_{QC_{-it}, I_{-i}, \varepsilon_{t}} 1(\sum_{j \neq i} QC_{jt} - \varepsilon_{t} \geq \\ &D_{t}(p) - \hat{S}_{it}^{1}(p)) dF(QC_{-it}, I_{-i}, \varepsilon_{t} | \hat{S}_{it}^{1}(p), k_{i} = 1, QC_{it}) \\ &= \int_{QC_{-it}, I_{-i}, \varepsilon_{t}} 1(\theta_{it} \geq \\ &D_{t}(p) - \hat{S}_{it}^{1}(p)) dF(QC_{-it}, I_{-i}, \varepsilon_{t} | \hat{S}_{it}^{1}(p), k_{i} = 1, QC_{it}) \end{split}$$

# We can do the same for type 2

But now

$$H_{it}(p, \hat{S}_{it}(p); k_i = 2, QC_{it}) = \int_{QC_{-it} \times I_{-i} \times \varepsilon_t} 1(\sum_{j \neq i \in I_0} QC_{jt} + \sum_{j \neq i \in I_1} S^1_{jt}(p, QC_{jt}) - \varepsilon_t \ge D_t(p) - \hat{S}^2_{it}(p)) dF(QC_{-it}, I_{-i}, \varepsilon_t | \hat{S}^2_{it}(p), k_i = 2, QC_{it})$$

$$= \int_{QC_{-it} \times I_{-i} \times \varepsilon_t} 1(\theta_{it} \ge 1) dP(QC_{-it}, I_{-i}, \varepsilon_t | \hat{S}^2_{it}(p), I_{-i}, I_{-$$

 $D_t(p) - \hat{S}_{i:}^2(p) dF(\mathbf{OC}_{-it}, \mathbf{l}_{-i}, \varepsilon_t | \hat{S}_{i:}^2(p), k_i = 2, OC_{it})$ 

(4)

where, 
$$\theta_{it} = \sum_{j \neq i \in I_0} QC_{jt} + \sum_{j \neq i \in I_1} S^1_{it}(p, QC_{jt}) - \varepsilon_t$$
.

We can do this recursively for all types. • Back

 $\Gamma(\cdot)$ : the conditional distribution of  $\theta_{it}$  (conditional on N-1 type draws).

$$\Delta(l_{-i})$$
: the marginal distribution of the vector of rival firm types.

Then  $H(\cdot)$  becomes

$$H_{it}(p, \hat{S}_{it}(p); k_i, QC_{it}) = \int_{l_{-1}} \left[ 1 - \Gamma \left( D_t(p) - \hat{S}_{it}^k(p) \right) \right] \cdot \Delta(l_{-i})$$

And  $\frac{H_S}{H_m}$  becomes

$$\frac{H_{s}\left(p, S_{it}^{*}(p); k_{i}, QC_{it}\right)}{H_{p}\left(p, S_{it}^{*}(p); k_{i}, QC_{it}\right)} = \frac{\int_{l_{-i}} \gamma\left(D_{t}(p) - \hat{S}_{it}^{k}(p)\right) \cdot \Delta(l_{-i})}{-\int_{l_{-i}} \gamma\left(D_{t}(p) - \hat{S}_{it}^{k}(p)\right) D_{t}'(p)\Delta(l_{-i})}.$$

**Assumption 2:**  $\Delta(\cdot)$  is an independent multivariate Poisson distribution truncated at k-1, as given by Poisson Cognitive Hierarchy model.

**Assumption 3:**  $\Gamma_i$  is a uniform distribution. (We can relax but adds to computational burden)

First-order condition simplifies to the "inverse elasticity rule":

$$p - C'_{it} \left( \hat{S}^k_{it}(p) \right) = \frac{1}{-D'_t(p)} * \left[ \hat{S}^k_{it}(p) - QC_{it} \right] = \frac{1}{-RD'_t(p)} * \left[ \hat{S}^k_{it}(p) - QC_{it} \right],$$

where the second equality follows from the fact that  $RD(p) = D(p) + \varepsilon - \sum_{j \neq i} S_{jt}(p) = D(p) + \varepsilon - \sum_{j \neq i} QC_{jt}$ . Hence, RD'(p) = D'(p) for all p.

## Objective function

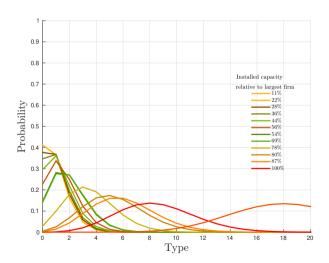
$$\omega(\hat{\gamma}) = \sum_{i} \sum_{t} \left[ \sum_{k} \left[ \sum_{p} \left( \frac{b_{it}^{\text{data}}(p) - b_{it}^{\text{model}}(p|k)}{b_{it}^{\text{model}}(p|K) - b_{it}^{\text{model}}(p|0)} \right)^{2} \times \mathbb{P}(p) \right] \mathbb{P}_{i}(k||K|, \hat{\gamma}) \right]$$

 $\mathbb{P}(p) \to \text{price points weighted by triangular distribution centered at market-clearing price}$ 

 $\mathbb{P}_i(k|\ |K|, \hat{\gamma}) \to \text{weight by probability of a firm being each type}$ 

# **Estimated Type Distributions**

$$k_i \sim Poisson(\hat{\tau}_i), \ \hat{\tau}_i = \exp(\hat{\gamma}_0 + \hat{\gamma}_1 \operatorname{size}_i + \hat{\gamma}_2 \operatorname{size}_i^2)$$



## Model fit: CH vs. Unilateral Best-Response

#### Dependent Variable: Profits from Actual Bids

	(1) CH Model	(2) Best-Response	(3)
Profits under Cognitive Hierarchy	0.803	-	0.642
	(0.069)	-	(0.127)
Profits under Best-Response	-	0.428	0.137
	-	(0.044)	(0.062)
Constant	-328.17	-241.74	-374.167
	(141.976)	(120.722)	(125.785)
Observations	1058	1058	1058
R <sup>2</sup>	0.67	0.49	0.69

Note: This table reports results from a regression of observed profits from actual bidding behavior on either firm profits as predicted by the Cognitive Hierarchy model (column 1), firm profits that would be achieved from a model of unilateral best-response to rival bids (column 2), or both. An observation is a firm-auction. Standard errors clustered at the firm-level are reported in parentheses.

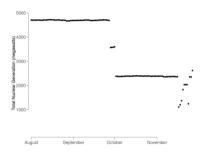
## More evidence on no learning

Offered Quantities into Market in Year 2 vs Year 1

	All Firms	All Firms	All Firms	Small Firms
	(1)	(2)	(3)	(4)
Year 2	-34.76	-15.85	-16.15	1.52
	(42.42)	(34.24)	(34.70)	(2.90)
Firm Fixed Effects	Yes	Yes	Yes	Yes
INC Fixed Effects	No	Yes	Yes	Yes
Day of Week Fixed Effects	No	No	Yes	Yes
Observations	2264	2264	2264	1029
$R^2$	0.01	0.03	0.04	0.09

 $<sup>^+</sup>$ p<0.05;  $^*$ p<0.01. The dependent variable *Participation Quantity*<sub>it</sub> is the megawatt quantity of output bid at the market-clearing price relative to the firm's contract position in auction t, i.e.  $|S_{it}(p^{mcp}) - QC_{it}|$ . The sample period is the first 1.5 years of the market and *Year* 2 is a dummy variable for the second year. Standard errors clustered at the firm-level are reported in parentheses.

# Corroborating "Reduced-Form" Evidence of Non-strategic Behavior Publicly Observable Shock – Nuclear Generator Went Off-line



#### Descriptive regressions find:

- Large firms respond to own cost shocks and cost shocks of competitors
- Small firms only respond to own cost shocks

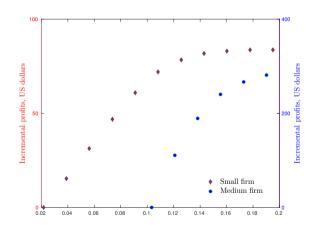
## Corroborating "Reduced-Form" Evidence of Non-strategic Behavior

	Largest Six	Smallest Six	Largest Six	Smallest Six	Largest Six	Smallest Six
Outage	-26.27*	-0.64	-9.80*	0.4	-8.40*	-0.03
	(4.69)	(0.42)	(2.92)	(0.38)	(2.05)	(0.25)
Own MC			0.27*	0.18*	0.30*	0.11*
			(0.03)	(0.02)	(0.03)	(0.02)
Constant	40.28*	3.75*	2.82	0.19	-21.13*	0.76*
	(4.49)	(0.32)	(2.41)	(0.37)	(6.55)	(0.21)
Bidder Fixed Effects	No	No	No	No	Yes	Yes
N	378	378	378	378	378	378
$R^2$	0.09	0.01	0.40	0.31	0.67	0.68

Note: Each column reports estimates from a separate regression of the slope of a firm's bid function on an indicator variable that the auction occurred during the fall 2002 nuclear outage. An observation is a firm-auction. The dependent variable is the slope  $(\frac{\partial S_{it}}{\partial p})$  of firm i's bid in auction t where the slope is linearized plus and minus \$10 around the market-clearing price. Own MC is the slope of the firm's own marginal cost function linearized plus and minus \$10 around the market-clearing price. White standard errors are reported in parentheses. + p<0.05, \* p<0.01

# Diminishing Returns to Sophistication

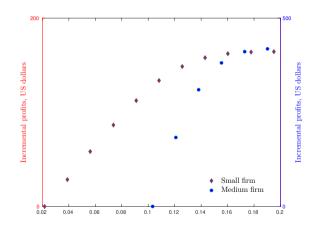
#### **INC** side



x-axis includes range from smallest to largest firm

# Diminishing Returns to Sophistication

#### **DEC** side



x-axis includes range from smallest to largest firm